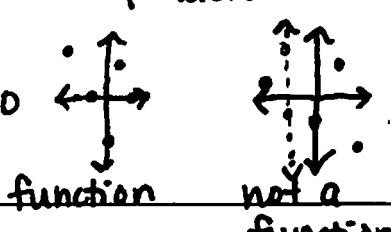


FUNCTIONS & LINEAR RELATIONSHIPS DICTIONARY

GRAPHING BASICS	DEFINITION	EXAMPLE OR VISUAL
COORDINATE PLANE	Formed by the intersection of two number lines, the horizontal axis and the vertical axis.	
X-AXIS	The horizontal axis on the coordinate plane.	
Y-AXIS	The vertical axis on the coordinate plane.	
QUADRANTS	The four regions into which the x and y-axis separate the coordinate plane.	
ORIGIN	The point at which the x and y-axis intersect on the coordinate plane. $(0,0)$	
ORDERED PAIR	The set of numbers, or coordinates, written in the form (x,y) .	
X-COORDINATE	The x-value of an ordered pair, represents the horizontal placement of the point.	
Y-COORDINATE	The y-value of an ordered pair, represents the vertical placement of the point.	

FUNCTIONS	DEFINITION	EXAMPLE OR VISUAL
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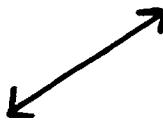
RELATION	A Set of ordered pairs.	$\{(5, -1), (-6, 2), (4, 0)\}$
DOMAIN	The set of x-values within the ordered pairs of a relation.	$\{5, -1\}, \{-6, 2\}, \{4, 0\}$ $D: \{-6, 4, 5\}$
RANGE	The set of y-values within the ordered pairs of a relation.	$\{5, -1\}, \{-6, 2\}, \{4, 0\}$ $R: \{-1, 0, 2\}$
FUNCTION	A relation in which each element of the domain is paired with exactly one element of the range. x's do not repeat	$\{5, -1\}, \{-6, 2\}, \{4, 0\}$ ↑ ↑ ↑ x's do not repeat
INDEPENDENT VARIABLE	The x-value within a function.	$y = mx + b$ ↑ independent
DEPENDENT VARIABLE	The y-value within a function.	$y = mx + b$ ↑ dependent
VERTICAL LINE TEST	If any vertical line passes through the graph of a relation no more than once, then it is a function.	

LINEAR EQUATIONS	DEFINITION	EXAMPLE OR VISUAL
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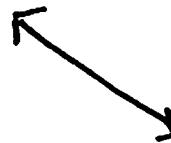
RATE OF CHANGE	A ratio that shows how one variable changes with respect to another.	\$ 7.50 / hr 23 mi / gal 31 ft / sec
----------------	--	--

SLOPE A ratio that compares the vertical to horizontal change between points. $m = \frac{\text{rise}}{\text{run}}$

POSITIVE SLOPE A line that is increasing from left to right.



NEGATIVE SLOPE A line that is decreasing from left to right.



ZERO SLOPE A horizontal line



UNDEFINED SLOPE A vertical line



SLOPE FORMULA A formula used to find the slope between 2 points. $m = \frac{y_2 - y_1}{x_2 - x_1}$

SLOPE-INTERCEPT FORM

The form of a line, used to graph the line.

$$y = mx + b$$

↑ ↑
slope y-intercept

STANDARD FORM

Another form of a line

$$Ax + By = C$$

VERTICAL LINE

A line with an undefined slope; $x = a$



HORIZONTAL LINE

A line with zero slope;
 $y = a$



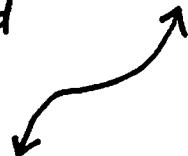
LINEAR FUNCTION

A function represented by a line; rate of change is constant



NONLINEAR FUNCTION

A function that cannot be represented by a line, but often is a curve; rate of change is not constant



DIRECT VARIATION

DEFINITION

EXAMPLE OR VISUAL

PROPORTIONAL RELATIONSHIP

If the ratios of quantities are equal, then they are proportional.

$$5 \text{ candies} = \$0.50 \\ 7 \text{ candies} = \$0.70$$

NONPROPORTIONAL RELATIONSHIP

If the ratios of quantities are not equal, then they are not proportional.

$$12 \text{ candies} = \$1 \\ 30 \text{ candies} = \$2$$

CONSTANT OF VARIATION

The ratio between all ordered pairs

$$k = \frac{y}{x}$$

DIRECT VARIATION

A specific relationship in which there is a constant ratio between all ordered pairs.

$$y = k \cdot x$$

COORDINATE PLANE

Formed by the intersection of two number lines, the horizontal axis and the vertical axis.

parts of the plane

x-axis
The horizontal axis

y-axis
The vertical axis

ORIGIN:

The point at which the x-axis and y-axis intersect ; $(0,0)$.

QUADRANTS:

The four regions into which the x and y-axis separate the coordinate plane.

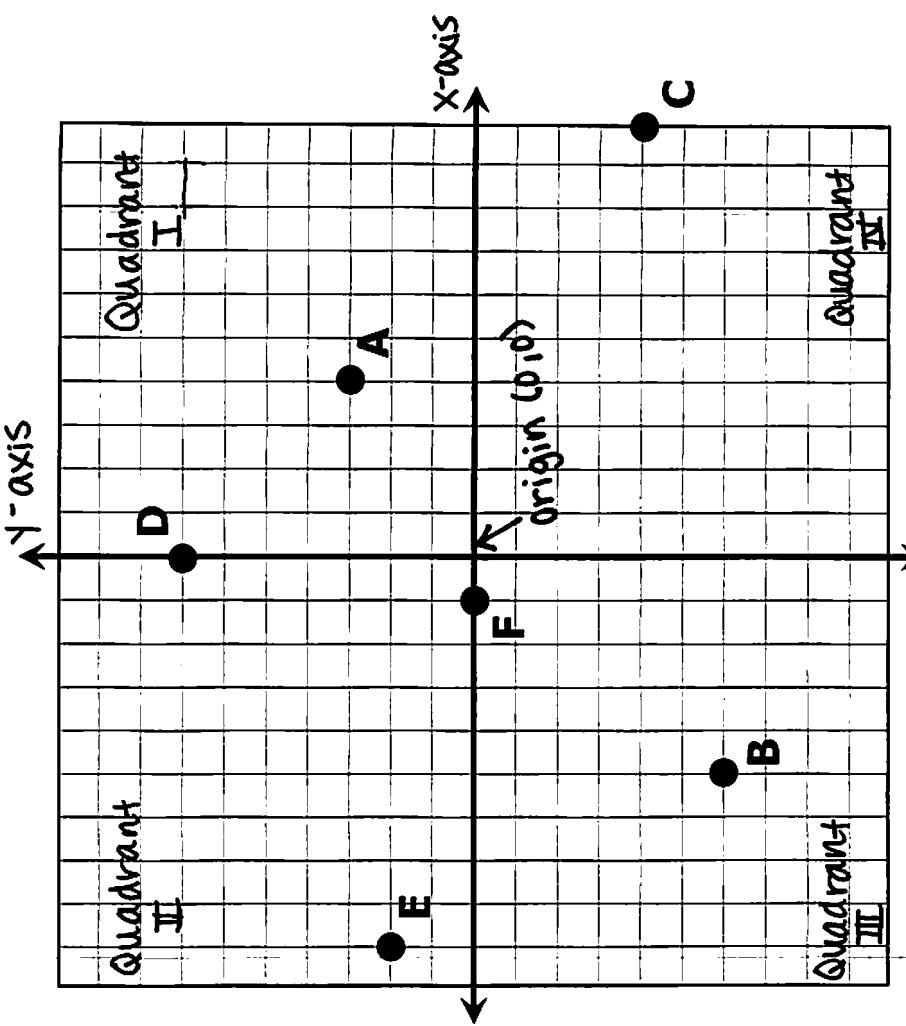
ORDERED PAIR:

A pair of numbers used to locate any point on the plane.

(X, Y)

X-coordinate

y-coordinate



LOCATING POINTS: Identify the ordered pair and quadrant (or axis) for each point.

POINT

ORDERED PAIR

A	$(4, 3)$
B	$(-5, -6)$
C	$(10, -4)$
D	$(0, 7)$
E	$(-9, 2)$
F	$(-1, 0)$

Name:

Date:

Topic:

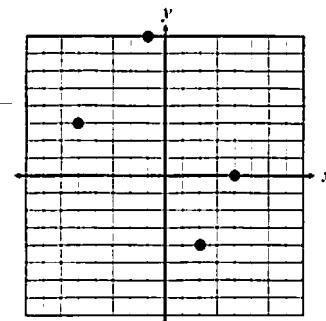
Class:

Main Ideas/Questions	Notes/Examples																																										
RELATION	<p>A set of ordered pairs.</p> <p>Example: $\{(-6, 2), (5, -1), (0, 6), (-4, 1)\}$</p> <p>Can be shown as: ordered pairs, tables, graphs</p>																																										
DOMAIN	The set of x-values within a relation.																																										
RANGE	The set of y-values within a relation.																																										
examples	<table border="1"> <thead> <tr> <th>ORDERED PAIRS</th> <th>TABLE</th> <th>GRAPH</th> </tr> </thead> <tbody> <tr> <td>① $\{(5, 2), (-7, 1), (0, 3), (4, -4)\}$</td><td> <table border="1"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>2</td> </tr> <tr> <td>-7</td> <td>1</td> </tr> <tr> <td>0</td> <td>3</td> </tr> <tr> <td>4</td> <td>-4</td> </tr> </tbody> </table> Domain: $\{-7, 0, 4, 5\}$ Range: $\{-4, 1, 2, 3\}$ </td><td> </td></tr> <tr> <td>② $\{(-6, 0), (1, 4), (8, -3), (1, -5)\}$</td><td> <table border="1"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>-6</td> <td>0</td> </tr> <tr> <td>1</td> <td>4</td> </tr> <tr> <td>8</td> <td>-3</td> </tr> <tr> <td>1</td> <td>-5</td> </tr> </tbody> </table> Domain: $\{-6, 1, 8\}$ Range: $\{-5, -3, 0, 4\}$ </td><td> </td></tr> <tr> <td>③ For questions 3 and 4, use the points plotted on the graph.</td><td> $\{(-6, -5), (0, -7), (2, 4), (4, -7)\}$ Domain: $\{-6, 0, 2, 4\}$ Range: $\{-7, -5, 4\}$ </td><td> <table border="1"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>-6</td> <td>-5</td> </tr> <tr> <td>0</td> <td>-7</td> </tr> <tr> <td>2</td> <td>4</td> </tr> <tr> <td>4</td> <td>-7</td> </tr> </tbody> </table> </td></tr> </tbody> </table>	ORDERED PAIRS	TABLE	GRAPH	① $\{(5, 2), (-7, 1), (0, 3), (4, -4)\}$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>2</td> </tr> <tr> <td>-7</td> <td>1</td> </tr> <tr> <td>0</td> <td>3</td> </tr> <tr> <td>4</td> <td>-4</td> </tr> </tbody> </table> Domain: $\{-7, 0, 4, 5\}$ Range: $\{-4, 1, 2, 3\}$	x	y	5	2	-7	1	0	3	4	-4		② $\{(-6, 0), (1, 4), (8, -3), (1, -5)\}$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>-6</td> <td>0</td> </tr> <tr> <td>1</td> <td>4</td> </tr> <tr> <td>8</td> <td>-3</td> </tr> <tr> <td>1</td> <td>-5</td> </tr> </tbody> </table> Domain: $\{-6, 1, 8\}$ Range: $\{-5, -3, 0, 4\}$	x	y	-6	0	1	4	8	-3	1	-5		③ For questions 3 and 4, use the points plotted on the graph.	$\{(-6, -5), (0, -7), (2, 4), (4, -7)\}$ Domain: $\{-6, 0, 2, 4\}$ Range: $\{-7, -5, 4\}$	<table border="1"> <thead> <tr> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>-6</td> <td>-5</td> </tr> <tr> <td>0</td> <td>-7</td> </tr> <tr> <td>2</td> <td>4</td> </tr> <tr> <td>4</td> <td>-7</td> </tr> </tbody> </table> 	x	y	-6	-5	0	-7	2	4	4	-7
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2	4																																										
4	-7																																										

4

$$\{(-5, 3), (-1, 8), (2, -4), (4, 0)\}$$

x	y
-5	3
-1	8
2	-4
4	0

Domain: $\{-5, -1, 2, 4\}$ Range: $\{-4, 0, 3, 8\}$ **FUNCTION**

A relation is a function if each x-value is paired with one + only one y-value.

Directions: Determine whether each relation is a function.

examples

5

$$\{(6, -2), (-4, -1), (2, 0), (-7, 4)\}$$

yes

6

$$\{(1, 5), (-5, -3), (-8, -1), (1, -7)\}$$

no

7

$$\{(1, 4), (2, 4), (3, 4), (4, 4)\}$$

yes

8

$$\{(-7, 4), (-4, 1), (-4, -9), (0, -6)\}$$

no

9

x	y
-2	4
-1	1
0	0
1	1
2	4

yes

10

x	y
-7	0
-4	1
-1	2
5	3
8	4

yes

11

x	y
-3	-2
-3	-1
-3	0
-3	5
-3	9

no

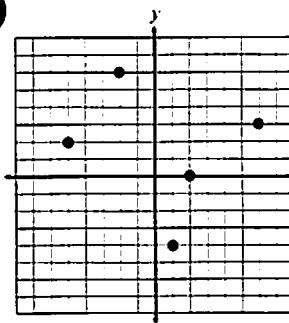
VERTICAL LINE TEST

When given the graph of a relation, the vertical line test can be used to determine whether the relation is a function.

Vertical Line Test: If any vertical line passes through the graph of a relation no more than once, then its a function.

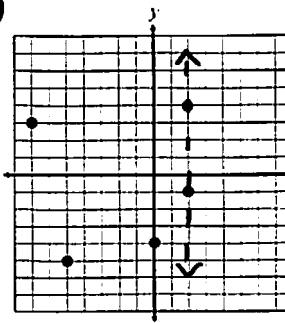
examples

12



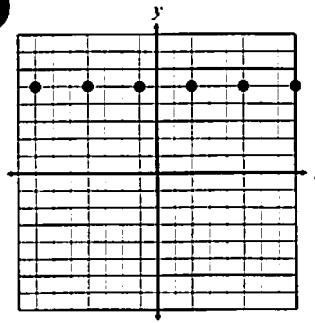
yes

13



no

14



yes

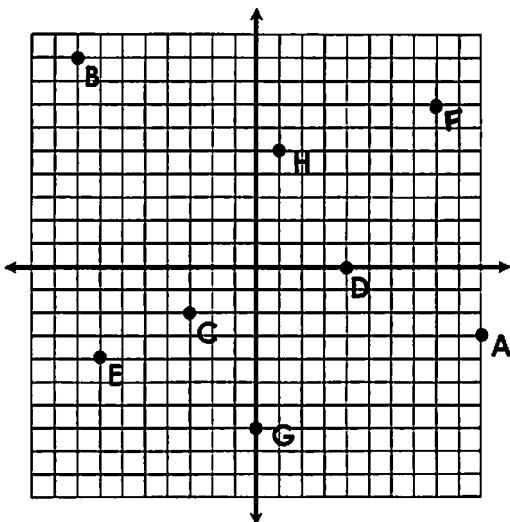
Name: _____

Unit 5: Functions & Linear Relationships

Date: _____ Per: _____

Homework 1: Coordinate Plane, Relations, & Functions**** This is a 2-page document! ****

1. Identify the ordered pair and quadrant (or axis) for each point on the graph.



Point	Ordered Pair	Quadrant
A	(10, -3)	IV
B	(-8, 9)	II
C	(-3, -2)	III
D	(4, 0)	x-axis
E	(7, -4)	III
F	(8, 7)	I
G	(0, -7)	y-axis
H	(1, 5)	I

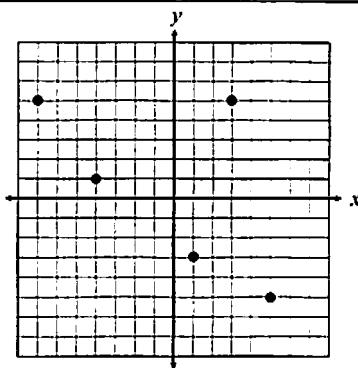
Directions: For questions 2 and 3, complete the table and graph for each relation. Then give the domain and range. For questions 4 and 5, give the ordered pairs and complete the table for the relation shown on the graph. Then give the domain and range.

ORDERED PAIRS	TABLE	GRAPH												
2. $\{(4, -1), (6, 2), (-7, -6), (-5, 2), (-1, -8)\}$	<table border="1"> <thead> <tr> <th>x</th><th>y</th></tr> </thead> <tbody> <tr> <td>4</td><td>-1</td></tr> <tr> <td>6</td><td>2</td></tr> <tr> <td>-7</td><td>-6</td></tr> <tr> <td>-5</td><td>2</td></tr> <tr> <td>-1</td><td>-8</td></tr> </tbody> </table>	x	y	4	-1	6	2	-7	-6	-5	2	-1	-8	
x	y													
4	-1													
6	2													
-7	-6													
-5	2													
-1	-8													
Domain: $\{-7, -5, -1, 4, 6\}$	Range: $\{-8, -6, -1, 2\}$													
3. $\{(-4, -1), (0, 3), (-2, -7), (8, 5), (2, -6)\}$	<table border="1"> <thead> <tr> <th>x</th><th>y</th></tr> </thead> <tbody> <tr> <td>-4</td><td>-1</td></tr> <tr> <td>0</td><td>3</td></tr> <tr> <td>-2</td><td>-7</td></tr> <tr> <td>8</td><td>5</td></tr> <tr> <td>2</td><td>-6</td></tr> </tbody> </table>	x	y	-4	-1	0	3	-2	-7	8	5	2	-6	
x	y													
-4	-1													
0	3													
-2	-7													
8	5													
2	-6													
Domain: $\{-4, -2, 0, 2, 8\}$	Range: $\{-6, -1, 3, 5, 7\}$													

4.

$$\{(-7, 5), (-4, 1), (1, -3), (3, 5), (5, -5)\}$$

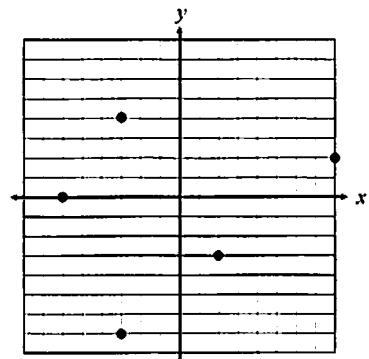
x	y
-7	5
-4	1
1	-3
3	5
5	-5

Domain: $\{-7, -4, 1, 3, 5\}$ Range: $\{-5, -3, 1, 5\}$

5.

$$\{(-6, 0), (-3, 4), (-3, -1), (2, -3), (8, 2)\}$$

x	y
-6	0
-3	4
-3	-1
2	-3
8	2

Domain: $\{-6, -3, 2, 8\}$ Range: $\{-1, -3, 0, 2, 4\}$ **Directions:** Determine whether each relation is a function.

6. $\{(5, 12), (\underline{-4}, 9), (\underline{-2}, -7), (\underline{-4}, 0), (3, 2)\}$

no

7. $\{(\underline{-1}, 1), (\underline{-2}, 3), (\underline{-3}, 5), (\underline{-4}, 7), (\underline{-5}, 9)\}$

yes

8.

x	-8	-4	0	4	8
y	5	1	-2	1	5

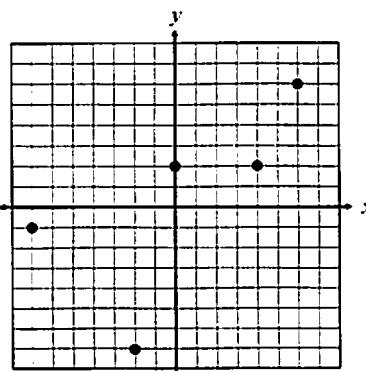
yes

9.

x	7	7	7	7	7
y	0	-5	-8	4	3

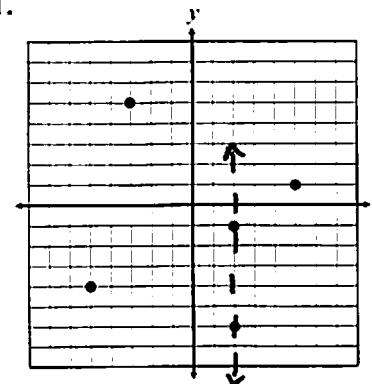
no

10.



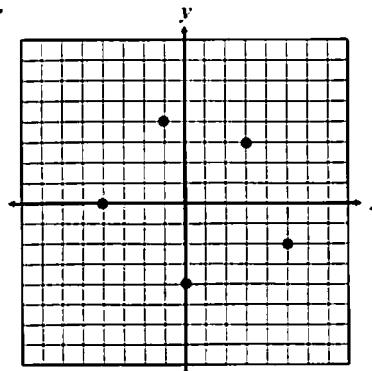
yes

11.



no

12.



yes